LatentLLM: Attention-Aware Joint Tensor Compression

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Abstract

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Abstract

We propose a new framework to convert a large foundation model such as large language models (LLMs)/large multimodal models (LMMs) into a reduced-dimension latent structure. Our method uses a global attention-aware joint tensor decomposition to significantly improve the model efficiency. We show the benefit on several benchmark including multi-modal reasoning tasks.

1. Introduction

Large language models (LLMs) [1, 27] and large multimodal models (LMMs) [19] have shown excellent performance across a variety of general tasks [4, 14, 29]. Nonetheless, these models having billions of parameters demand significant computational resources [25]. Towards increasing the accessibility of LLMs/LMMs for limited resource devices, extensive efforts have been devoted to model compression [2, 30, 34]: e.g., partial activation [13, 16], pruning [3, 8, 10, 26], quantization [9, 17, 28], distillation [6, 11, 12], and low-rank factorization [12, 18, 32].

Recently DeepSeek-V3 [18] has attracted much attention for its high efficiency with latent reduction. It employs a multi-head latent attention (MLA) to compress the multihead attention (MHA), realizing an efficient KV cache [5]. In this paper, we provide a novel solution to convert a pretrained LLM/LMM built with MHA into a compressed LLM/LMM with MLA. Our approach is motivated by a global compression framework [3, 28], while we adopt it for tensor rank reduction not for pruning or quantization. Our derived solution is based on a high-order tensor-rank decomposition to jointly factorize multiple layers.

The contributions of our paper are summarized below.

- We propose a novel low-rank decomposition approach called LatentLLM to compress LLMs/LMMs.
- We discuss an optimal pre-conditioning for activationaware SVD.
- We reveal that a choice of junction matrix can significantly reduce the model size.



Figure 1. Reduced-dimension LLM/LMM with low-rank tensor decomposition. (a) each module is locally compressed. (b) multiple modules are globally compressed.

- We then introduce an attention-aware joint SVD framework to compress multiple weights at the same time.
- Our experiments validate that our LatentLLM approach can improve the efficiency of LLM/LMM.
- The latent LLaVA with our method offers a significant advantage in multi-modal reasoning capability.

2. LatentLLM: Tensor compression

2.1. Reduced-dimension LLM/LMM

Fig. 1 illustrates the basic transformer architecture consisting of MHA and MLP, used in typical LLMs/LMMs. For MLP, there are up and down projections, whereas MHA has query/key/value/output projections. By transforming those dense weight matrices into low-rank decompositions, we can realize an efficient latent LLM/LMM having potential benefits: (i) fewer-parameter model size; (ii) KV cache reduction; (iii) accelerated processing; (iv) lowerpower consumption. In fact, some recent LLM models such as DeepSeek-V3 [18] demonstrated efficiency and highperformance with MLA. We focus on compressing a pretrained LLM/LMM by converting MHA into MLA in a

Table 1. Variants of pre-conditioning matrices P.

Conditioning P	Expression
Identity (Plain SVD) [7, 24]	Ι
Diagonal Hessian [8-10]	$diag[(XX^\top + \lambda I)^{-1}]^{\frac{-1}{2}}$
Diagonal ℓ_1 -norm [17, 32]	$\operatorname{diag}\left[\sum_{j} X_{1,j} , \ldots, \sum_{j} X_{d,j} \right]^{\alpha}$
Diagonal ℓ_2 -norm [26]	$diag[XX^{\top}]^{\frac{1}{2}}$
Covariance [31]	$XX^{\top} + \lambda I$
Root-Covariance (Ours)	$(XX^{\top} + \lambda I)^{\frac{1}{2}}$

zero-shot fashion, i.e., without any fine-tuning.

Most existing methods are based on a local optimization to approximate each weight individually. Motivated by recent global optimization [3, 28], we propose a joint tensor compression method that we call "LatentLLM." Before describing our solution, we first address activation-aware compression to provide some new insights below.

2.2. Activation-aware SVD: Pre-conditioning

A pioneering work by ASVD [32] introduced a way to compress a layer depending on the activation statistics. Consider a pretrained-weight $W \in \mathbb{R}^{d' \times d}$ to compress with a lower-rank decomposition $\hat{W} = BA$ for compression matrix $A \in \mathbb{R}^{r \times d}$ and decompression matrix $B \in \mathbb{R}^{d' \times r}$. Using the input activation $X \in \mathbb{R}^{d \times l}$ (*l* is the calibration sample length), ASVD aims to minimize the activation loss:

$$\mathcal{L}_1 = \mathbb{E}_X \left\| WX - \hat{W}X \right\|^2 = \mathbb{E}_X \left\| WX - BAX \right\|^2, \quad (1)$$

instead of the naïve weight-based loss: $\mathcal{L}_0 = ||W - \hat{W}||^2$. While the optimal solution to minimize \mathcal{L}_0 can be given by the plain SVD of W, to minimize \mathcal{L}_1 , ASVD introduced a pre-conditioning matrix $P \in \mathbb{R}^{d \times d}$ to whiten the statistical impact of the activation X. Specifically, ASVD uses the low-rank matrices given by whitened SVD:

$$BAP = \mathsf{svd}_r[WP],\tag{2}$$

where $\operatorname{svd}_r[\cdot]$ denotes the rank-*r* truncated SVD.

The optimal pre-conditioning matrix P can be given by reformulating \mathcal{L}_1 as follows:

$$\mathcal{L}_1 = \operatorname{tr}\left[(W - BA) \mathbb{E}_X [XX^\top] (W - BA)^\top \right]$$
(3)

$$= \left\| (W - BA)C^{\frac{1}{2}} \right\|^{2} = \left\| WC^{\frac{1}{2}} - BAC^{\frac{1}{2}} \right\|^{2}, \quad (4)$$

where $C = \mathbb{E}_X[XX^{\top}] \in \mathbb{R}^{d \times d}$ is a covariance of input activation. Hence, the above loss can be minimized by the SVD: $BAC^{\frac{1}{2}} = \operatorname{svd}_r[WC^{\frac{1}{2}}]$. Accordingly, it is found that the optimal pre-conditioner is the square-root covariance: $P = C^{\frac{1}{2}}$. Given the finite calibration data X, we can estimate the covariance as $C = XX^{\top} + \lambda I$, where the damping factor $\lambda \in \mathbb{R}_+$ corresponds to the shrunk estimator [15].

Remark 1 Different pre-conditioning was introduced for pruning and quantization, as listed in Tab. 1.



Figure 2. Activation-aware compression with pre-conditioning and junction matrix. The junction matrix J can be adjusted to save the number of parameters and inference computation.

2.3. Junction matrix for model compression

The solution of Eq. (2) has non-unique decomposition for matrices B and A. Consider the truncated SVD written as $USV = \text{svd}_r[WP]$, where $U \in \mathbb{R}^{d' \times r}$, $S \in \mathbb{R}^{r \times r}$, and $V \in \mathbb{R}^{r \times d}$ are the left singular unitary matrix, singular-value diagonal matrix, and right singular unitary matrix, respectively. Hence, the matrices B and A can be expressed:

$$B = USJ, \qquad A = J^+ VP^+, \tag{5}$$

where $J \in \mathbb{R}^{r \times r}$ is a junction matrix and $[\cdot]^+$ denotes the pseudo inverse. Choosing any junction matrix that satisfies $SJJ^+ = S$ has no impact on the loss. Hence, there is few literature discussing the choice of J.

However, a certain choice of J has a noticeable advantage to reduce the number of parameters and floatingpoint operations (FLOPs). We can write the whitened right-singular matrix VP^+ as two sub-blocks: $VP^+ = [V_1 \quad V_2]$, for $V_1 \in \mathbb{R}^{r \times r}$ and $V_2 \in \mathbb{R}^{r \times (d-r)}$. When we use $J = V_1$, the compression matrix A will contain an identity block as long as V_1 is non-singular:

$$A = J^{+}VP^{+} = V_{1}^{+} \begin{bmatrix} V_{1} & V_{2} \end{bmatrix} = \begin{bmatrix} I & V_{1}^{+}V_{2} \end{bmatrix}.$$
 (6)

This can greatly reduce the number of parameters from r(d'+d) to $r(d'+d)-r^2$, as well as the FLOPs, because no computation is needed for the identity projection. Fig. 2 depicts the role of the pre-conditionning and junction matrices for the activation-aware compression, showing the flexibility of tensor mapping with the tensor diagrams.

Remark 2 Pivoting columns solves the case when V_1 is singular, without additional FLOPs in inference.

3. LatentLLM: Joint tensor compression

The SVD described above is optimal in the sense that the local error is minimized for the single tensor compression,



Figure 3. Tucker decomposition for joint QK compression.

whereas it does not guarantee global optimality. Motivated by SparseLLM [3], we propose a joint tensor compression technique which factorizes multiple tensors concurrently.

3.1. Multi-head latent attention: Joint QK SVD

First, we consider a joint compression of query (Q) and key (K) projections in MHA to convert into MLA. The attention map is the dot product of query and key features: $M_i = X^{\top}W_{q,i}^{\top}W_{k,i}X$, where $M_i \in \mathbb{R}^{l \times l}$ is the *i*th head attention map before softmax operation, $W_{q,i} \in \mathbb{R}^{d_h \times d}$ is the *i*th head query projection matrix, and $W_{k,i} \in \mathbb{R}^{d_h \times d}$ is the *i*th head key projection matrix. Here, d_h is the head dimension, which is often $d_h = d/h$ for the number of heads h.

We consider minimizing the attention map error:

$$\mathcal{L}_{2} = \sum_{i=1}^{h} \left\| M_{i} - X^{\top} A_{q}^{\top} B_{q,i}^{\top} B_{k,i} A_{k} X \right\|^{2},$$
(7)

where $A_{q} \in \mathbb{R}^{r_{q} \times d}$ is for the Q compression, $A_{k} \in \mathbb{R}^{r_{k} \times d}$ is for the K compression, $B_{q,i} \in \mathbb{R}^{d_{h} \times r_{q}}$ is for the *i*th head Q decompression, and $B_{k,i} \in \mathbb{R}^{d_{h} \times r_{k}}$ is for the *i*th head K decompression, respectively. Here, r_{q} and r_{k} are the latent dimensions for Q and K. Similar to Eq. (4), we can rewrite:

$$\mathcal{L}_{2} = \sum_{i=1}^{h} \left\| G_{i} - A_{q}^{\prime \top} H_{i} A_{k}^{\prime} \right\|^{2},$$
(8)

where $G_i = C^{\frac{1}{2}} W_{q,i}^{\top} W_{k,i} C^{\frac{1}{2}}$, $A'_q = A_q C^{\frac{1}{2}}$, $A'_k = A_k C^{\frac{1}{2}}$, and $H_i = B_{q,i}^{\top} B_{k,i}$ This is known as a high-order SVD (HOSVD) problem to decompose for the 3-mode tensor $G \in \mathbb{R}^{h \times d \times d}$, whose *i*th slice is G_i . A'_q corresponds to the 2nd tensor plane, A'_k is the 3rd tensor plane, and $H \in \mathbb{R}^{h \times r_q \times r_k}$, whose *i*th slice is H_i , is the tensor core.

This is illustrated in Fig. 3. This Tucker tensor decomposition is typically solved by alternating SVD over each slice sequentially. Algorithm 1 shows the pseudo-code of the joint SVD compression for QK latent projections. Here, we generalize the pre-conditioning matrix P, as not necessarily the optimal $C^{\frac{1}{2}}$. In addition, we explicitly denoted any arbitrary junction matrices that do not change the error. Note that there are additional junction matrices per heads $J_i \in \mathbb{R}^{d_h \times d_h}$ as well as individual Q/K junctions $J_q \in \mathbb{R}^{r_k \times r_k}$ and $J_k \in \mathbb{R}^{r_k \times r_k}$. This suggests that we can further reduce the number of parameters by transforming into the block identity form per head.

Algorithm 1 Joint SVD for QK Projections in MHA

Input: Pre-conditioning $P \in \mathbb{R}^{d \times d}$, query projection heads $W_{q,i} \in \mathbb{R}^{d_h \times d}$, key projection heads $W_{k,i} \in \mathbb{R}^{d_h \times d}$, number of heads h, rank r_q, r_k , iteration N **Initialize:** $W_{q,i} = W_{q,i}P$ for $i \in \{1, \dots, h\}$ $W_{k,i} = W_{k,i}P$ for $i \in \{1, \dots, h\}$ $G_i = W_{q,i}^\top W_{k,i}$ for $i \in \{1, \dots, h\}$ $A_q = \text{RightSingular}_{r_q} \left[\sum_{i=1}^h G_i G_i^\top \right]$ **for** n = 1 **to** N **do** $A_k = \text{RightSingular}_{r_q} \left[\sum_{i=1}^h G_i A_q^\top A_q G_i \right]$ $A_q = \text{RightSingular}_{r_q} \left[\sum_{i=1}^h G_i A_k A_k^\top G_i^\top \right]$ **end for Output:** $B_{q,i} = J_i^\top W_{q,i} A_q^\top J_q$ for $i \in \{1, \dots, h\}$ $B_{k,i} = J_i^+ W_{k,i} A_k^+ J_k$ for $i \in \{1, \dots, h\}$ $A_q = J_q^+ A_q P^+$ $A_k = J_k^+ A_k P^+$

3.2. Multi-head latent attention: Joint VO SVD

Next, we discuss the joint SVD for value (V) and output (O) projections in MHA. For any arbitrary attention map, we may consider minimizing the loss:

$$\mathcal{L}_{3} = \sum_{i=1}^{h} \left\| W_{\mathrm{o},i} W_{\mathrm{v},i} X - \hat{W}_{\mathrm{o},i} \hat{W}_{\mathrm{v},i} X \right\|^{2}, \qquad (9)$$

where $W_{o,i} \in \mathbb{R}^{d' \times d_h}$ is the *i*th head output projection, and $W_{v,i} \in \mathbb{R}^{d_h \times d}$ is the *i*th head value value projection. Here we design the low-rank compression: $\hat{W}_{o,i} = B_o A_{o,i} \in \mathbb{R}^{d' \times d_h}$ and $\hat{W}_{v,i} = B_{v,i}A_v \in \mathbb{R}^{d_h \times d}$ with $B_o \in \mathbb{R}^{d' \times r_o}$, $A_{o,i} \in \mathbb{R}^{r_o \times d_h}$, $B_{v,i} \in \mathbb{R}^{d_h \times r_v}$, and $A_v \in \mathbb{R}^{r_v \times d}$. Interestingly, this is also formulated in a similar manner of Eq. (8), and it can be solved by the joint SVD algorithm.

3.3. Latent MLP: Joint UD SVD

Finally, we address the joint compression of MLP layers which consists of up (U) projection and down (D) projection in typical LLMs/LMMs. Although the global optimization is generally difficult due to the nonlinear activations in the MLP layer, SparseLLM [3] provides an elegant way to approximate MLP layer. The key idea is to minimize the MLP loss in a decoupled manner by introducing auxiliary variables. Our LatentLLM exploits the same philosophy to compress MLP layers not to prune. Refer more details on the decoupled optimization in SparseLLM [3].

4. Experiments

We conduct experiments for LLM and LMM benchmarks to evaluate the effectiveness of our method, based on the same setting of SparseLLM [3] and their code base¹. For LLM

https://github.com/BaiTheBest/SparseLLM



Figure 4. Perplexity (\downarrow) over compression ratio for OPT models.

Table 2. Accuracy in percent (\uparrow) on ScienceQA dataset of LLaVA model with different compression methods for 10%–20% size reduction. Question subjects: natural science (NAT); social science (SOC); language science (LAN). Context modality: text (TXT); image (IMG); or no context (NO). Grades: 1–6 (G1-6); 7–12 (G7-12).

		Subject			Context Modality			Grades		
Method	Compression	NAT	SOC	LAN	TXT	IMG	NO	G1-6	G7-12	Avg
Original un-compressed	0%	72.47	69.18	65.73	73.51	68.82	65.99	72.72	65.19	70.03
Plain SVD (Identity)	10%	5.33	1.35	0.27	5.77	6.69	0.00	3.30	2.97	3.18
ASVD (Hessian)	10%	17.23	24.97	3.18	18.43	29.55	2.16	17.40	11.27	15.21
ASVD (ℓ_2 -norm)	10%	16.70	18.34	2.55	17.89	24.34	2.23	16.04	8.57	13.37
ASVD (Cov)	10%	41.21	27.22	37.91	41.30	35.15	38.33	38.62	35.27	37.42
ASVD (RootCov)	10%	64.08	56.13	57.36	64.03	60.98	57.35	62.70	57.02	60.67
LatentLLM (RootCov)	10%	68.52	64.23	61.36	69.06	65.20	61.53	68.72	60.45	65.76
Plain SVD (Identity)	20%	0.18	0.00	0.00	0.20	0.20	0.00	0.04	0.20	0.09
ASVD (Hessian)	20%	3.82	2.81	0.00	3.62	5.30	0.14	3.01	1.91	2.62
ASVD (ℓ_2 -norm)	20%	0.44	0.79	0.00	0.39	0.79	0.07	0.51	0.20	0.40
ASVD (Cov)	20%	41.39	27.22	37.55	41.45	35.35	38.12	38.69	35.14	37.42
ASVD (RootCov)	20%	61.19	53.43	53.36	61.53	59.40	52.68	58.96	54.98	57.53
LatentLLM (RootCov)	20%	66.39	61.19	60.82	67.20	63.41	60.62	66.41	59.26	63.85

calibration, we use 64 samples of 2048-token segments, randomly chosen from the first shard of the C4 [23] dataset. For LMM calibration, we use 64 samples, randomly chosen from the train split of the ScienceQA [20] dataset.

For LLM, we consider the OPT model family [33] as it provides a wide range of model scales from 125M to 175B. We consider the benchmark of raw-WikiText2 (WT2) [22], the Penn Treebank (PTB) [21], and the C4 [23], popular in the related literature [8, 9, 26]. For LMM, we use LLaVA 7B [19] model. We evaluate the capability of the multimodal answer reasoning with ScienceQA, which contains 21K questions for three subjects: natural, social, and language science. Some questions have image and/or text contexts, and the problem levels range from grade 1 to 12.

We first look into the compression capability of our LatentLLM for LLM benchmarks in Fig. 4. We can see that the conventional plain SVD has a poor performance, and that ASVD with a proper pre-conditioning can significantly improve the perplexity. Further, the joint SVD used for LatentLLM offers an additional improvement for all benchmarks.

We then show the accuracy of latent LLaVA models for ScienceQA multi-modal reasoning benchmark in Tab. 2. It is verified that our LatentLLM can significantly outperform other low-rank compression methods across diverse reasoning problems over different subjects/contexts/grades.

5. Summary

We introduced LatentLLM which jointly compresses multiple tensors through the use of high-order tensor-rank decomposition. We also provided new perspectives for choosing the pre-conditioner and junction matrix. Benchmark experiments demonstrated that the model compression performance of LLM/LMM can be significantly improved.

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